## Yousef Saad PHIDAL: A Parallel ILU factorization based on a Hierarchical Interface Decomposition

University of Minnesota Dept. of Computer Science and Engineering 200 Union st. SE Minneapolis MN 55455 saad@cs.umn.edu Pascal Henon

Ideas from domain decomposition have often been adapted and extended to derive parallel solution algorithms for sparse linear systems. The Parallel Hierarchical Interface Decomposition ALgorithm presented in this talk is in this category. The method is reminescent of the the 'wirebasket' techniques of domain decomposition methods [2] and can also be viewed as a variation and an extension of the pARMS algorithm [1] in which the independent sets and levels are defined from a hierarchical decomposition of the interface structure of the graph.

The algorithm is based on defining a 'hierarchical interface structure'. The hierarchy consists of classes with the property that Class k nodes, with k > 0, are separators for class k - 1 nodes. In each class, nodes are grouped in independent sets. Class 0 nodes are simply interior nodes of a domain in the graph partitioning of the problem. These are naturally grouped in group-independent sets. Nodes that are adjacent to more subdomains will be part of the higher level classes and are ordered last. The factorization uses dropping strategies which attempt to preserve the independent set structure.

One the hierarchical interface decomposition is defined, the Gaussian elimination process proceeds by levels: nodes of the first level are eliminated first, followed by those of the second level etc. All nodes of the first level can be eliminated independently - since there is no fill-in between nodes i and j of two different connectors of level 1. On the other hand fill-ins may appear between connectors at higher levels.

## Bibliography

- Z. Li, Y. Saad, and M. Sosonkina. pARMS: a parallel version of the algebraic recursive multilevel solver. *Numerical Linear Algebra with Applica*tions, 10:485–509, 2003.
- [2] B. Smith, P. Bjørstad, and W. Gropp. Domain decomposition: Parallel multilevel methods for elliptic partial differential equations. Cambridge University Press, New-York, NY, 1996.