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**Is the ideal approximation operator always “ideal” for a  
particular C/F splitting?**

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Given a coarse grid, the ideal prolongation operator is defined by  $\mathbf{P}_\star = [\mathbf{W} \ \mathbf{I}]^T$ , where the weight matrix,  $\mathbf{W} = \mathbf{A}_{FF}^{-1} \mathbf{A}_{FC}$ , interpolates a set of fine grid variable ( $F$ -points) from a set of coarse grid variable ( $C$ -points), and the identity matrix,  $\mathbf{I}$ , represents the injection of  $C$ -points to and from the coarse grid (Falgout and Vassilevski, 2004). In this talk, we consider  $\mathbf{P}_\star$ , constructed from both traditional  $C/F$  splittings and  $C/F$  splittings corresponding to aggregates, for several challenging problems. We demonstrate the effects of the  $C/F$  splitting on the convergence and complexity of  $\mathbf{P}_\star$ . Finally, we argue that  $\mathbf{P}_\star$  may be misleading in demonstrating the “ideal” nature of interpolation of a given  $C/F$  splitting by providing numerical evidence that hierarchies built using  $\mathbf{P}_\star$  converge more slowly than hierarchies built from alternative prolongation operators with the same  $C/F$  splitting. This is important as we wish to minimize the number of levels in a multigrid hierarchy by using a small set of  $C$  points for which  $\mathbf{P}_\star$  may have poor convergence.